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**Running head:** Estimating length of stay

**Short title:** Estimating the effect of MRSA infection on length of stay using a longitudinal model

**Abbreviations:** acute physiology and chronic health evaluation (APACHE), credible interval (CI), deviance information criterion (DIC), intensive care unit (ICU), Markov chain Monte Carlo (MCMC), Methicillin-resistant *Staphylococcus aureus* (MRSA), Methicillin-sensitive *Staphylococcus aureus* (MSSA), relative risk ratio (RRR), systemic inflammatory response syndrome (SIRS), therapeutic intervention scoring system (TISS)

**Word count:** 200 (abstract), 3975 (text)

## Abstract

Healthcare-associated methicillin-resistant *Staphylococcus aureus* (MRSA) infection may cause increased hospital stay or, sometimes, death. Quantifying this effect is complicated because it is a time-dependent exposure: infection may prolong hospital stay, while longer stays increase the risk of infection. We overcome these problems by using a multinomial longitudinal model for estimating the daily probability of death and discharge. We then extend the basic model to estimate how the effect of MRSA infection varies over time, and to quantify the number of excess ICU days due to infection. We find that infection decreases the relative risk of discharge (relative risk ratio = 0.68, 95% credible interval: 0.54, 0.82), but is only indirectly associated with increased mortality. An infection on the first day of admission resulted in a mean extra stay of 0.3 days (95% CI: 0.1, 0.5) for a patient with an APACHE II score of 10, and 1.2 days (95% CI: 0.5, 2.0) for a patient with an APACHE II score of 30. The decrease in the relative risk of discharge remained fairly constant with day of MRSA infection, but was slightly stronger closer to the start of infection. These results confirm the importance of MRSA infection in increasing ICU stay, but suggest that previous work may have systematically overestimated the effect size.

**Medical Subject Headings (MeSH) (keywords):** Competing risks, Intensive Care, Longitudinal analysis, Nosocomial Infections, Time-dependent

1 Healthcare associated infections affect 5–10% of acute-care patients in  
2 developed countries, and considerably more in developing nations (1). These  
3 infections are direct causes of patient morbidity and mortality, and are also  
4 believed to lead to increased hospital stays. Many infections are preventable  
5 by the use of interventions (2). Infections places an important—but poorly  
6 quantified—burden on health services. Quantifying excess hospital stay is  
7 essential for assessing how many bed days might be gained from preven-  
8 tion and subsequent health economic analyses that inform the allocation of  
9 resources to infection control programmes (3). The recent decision by the  
10 Centers for Medicare and Medicaid Services to stop re-imbursements to US  
11 hospitals for selected healthcare associated infections increases the need for a  
12 valid interpretation of the costs and benefits of infection control interventions  
13 (4).

14 Estimating additional length of hospital stay due to nosocomial infec-  
15 tions creates a number of statistical challenges (5). The central difficulty  
16 arises from the fact that infections may increase the length of stay, and in-  
17 creased length of stay simultaneously increases the chance of infection (6).  
18 However, most standard regression analyses assume a one-way direction of  
19 causation from exposure (infection) to response (length of stay). Standard  
20 survival analysis of hospital stay data is also inappropriate because censor-  
21 ing of hospital stays due to death does not occur at random. Instead, the  
22 most severely ill will have the highest chance of dying and the lowest chance  
23 of being discharged on a given day. Such informative censoring violates the

assumptions of standard survival analyses, and can lead to very large biases if unaccounted for. A further problem is that factors that may predispose a patient to infection (such as use of invasive interventions) may also be independently associated with increased length of stay.

In this paper we aim to address all these challenges, and to use individual patient-level data to quantify the additional length of stay in an intensive care unit (ICU) due to infections with one of the most virulent and widely distributed nosocomial pathogens, methicillin-resistant *Staphylococcus aureus* (MRSA).

We make use of a multinomial regression model with a longitudinal data format. This format has the advantage of allowing the use of time-dependent exposures (i.e. exposures such as assisted ventilation that may change during a patient's stay). Time-dependent exposures can be more informative than time-independent exposures because they offer the chance to examine the order of exposure and response.

A further advantage of the longitudinal format is that the effect of time-dependent exposures can be allowed to change over time by using time-dependent covariates. If modelled with only time-*independent* covariates, a hospital acquired infection would be assumed to decrease the risk of discharge by the same amount regardless of the length of time the patient had already spent in the ward. In contrast, time-dependent covariates allow changes in the exposure effects over time. Thus, for example, the effect of a nosocomial infection on the chances of being discharged might be strongest on the actual

47 day of infection and then wane over time.

48 The use of time-dependent exposures has been extensively studied in the  
49 field of longitudinal analyses (7, chapter 12) and in this paper we apply some  
50 of this knowledge to length of stay data.

## 51 MATERIALS AND METHODS

### 52 Clinical setting

53 Data were collected from all patients admitted to two adjacent 15 bed in-  
54 tensive care units (ICUs) in a 1100 bed dual-site teaching hospital in the  
55 United Kingdom between January 1st 2002 and April 20th 2006. During  
56 the study period 60% of the patients were medical, 21% surgical and 19%  
57 cardiothoracic. Data comprised age, sex, date of admission and discharge  
58 to ICU, speciality, day 1 Acute Physiology and Chronic Health Evaluation  
59 (APACHE)-II score, daily therapeutic intervention scoring system (TISS)  
60 score (8) which included measurements required to diagnose a systemic in-  
61 flammatory response syndrome, dates of starting or stopping ventilation or  
62 hemofiltration, date of collection and culture of MRSA from all microbiolog-  
63 ical samples, and date of starting treatment with vancomycin or linezolid.  
64 Clinical samples were only taken when local or systemic infection was sus-  
65 pected. Further details on infection control and laboratory practice have  
66 been previously reported (9, 10).

67 An MRSA infection was considered to be present if (and only if) three

68 conditions were satisfied: 1) MRSA was isolated from a sterile or non-sterile  
69 clinical sample including a removed vascular catheter tip; 2) there was treat-  
70 ment with vancomycin or linezolid which were the only antibiotics used for  
71 initial treatment of suspected or proven MRSA infection, started between  
72 1 day before and 3 days after the positive culture; and 3) there was a sys-  
73 temic inflammatory response syndrome (SIRS) response, requiring 2 of the  
74 following criteria present between 2 days before and 3 days after the positive  
75 MRSA culture: temperature  $< 36^{\circ}\text{C}$  or  $> 38^{\circ}\text{C}$ ; heart rate  $> 90$  bpm;  
76 respiratory rate  $> 20$  breaths/min or  $\text{PaCO}_2 < 32$  mmHg; white blood cell  
77 count  $> 12,000$  or  $< 4,000$  cells/mm<sup>3</sup> (11). Patients from whom MRSA was  
78 isolated from any site but who did not fulfil these additional criteria were  
79 considered to be colonised with MRSA.

## 80 **Data quality control**

81 Data quality control mechanisms included automated range, logic and date  
82 checks. The integrity of the data extraction process was validated for com-  
83 pleteness and accuracy by manually comparing 5% of the electronic database  
84 with the original source data.

## 85 **Exposures**

86 We were motivated to fit a longitudinal model because the data have a num-  
87 ber of important time-dependent exposures. The most important being the

88 presence of an MRSA infection, because the primary research question was  
89 the impact of such infections on length of stay. We carried forward the effect  
90 of MRSA over time, so once a patient had an MRSA infection their status  
91 was “yes” for all subsequent days until discharge. This is because we expect  
92 the effect of an infection to persist; how long the effect persists was one of  
93 the questions we addressed in the time-dependent covariate model. The list  
94 of exposures is in Table 1.

## 95 **Ethics approval**

96 The hospital ethics committee waived the need for patient consent and agreed  
97 to the use of this anonymised patient database for this study.

## 98 **Statistical methods**

99 Daily ICU data were used for all analyses. The table below shows a subset  
100 of the data for two subjects. Each of the  $n$  rows corresponds to one patient  
101 day on the ICU.



ICUID	Date	TISS	Sex	Outcome
3154	07 Feb 02	54	F	Stayed
3154	08 Feb 02	37	F	Stayed
3154	09 Feb 02	40	F	Stayed
3154	10 Feb 02	27	F	Discharged
3163	09 Feb 02	51	M	Stayed
3163	10 Feb 02	39	M	Stayed
3163	11 Feb 02	49	M	Stayed
3163	12 Feb 02	60	M	Died

Patient 3154 was admitted to the ICU on February 7th and discharged on the  
 10th, giving a length of stay of four days and a final outcome of “Discharged”.  
 Patient 3163 was admitted on February 9th and died on the 12th, giving  
 a length of stay of four days and a final outcome of “Died”. The TISS  
 score (a measure of the level of patient care required) is a time-dependent  
 exposure which changed from day-to-day (8). The nominal response variable  
 “Outcome” describes each patient’s day-to-day status (stayed, discharged or  
 died). We assumed this nominal response had a multinomial distribution,  
 and so examined the probability of “Stayed”, “Discharged” and “Died” for  
 the  $i$ th patient day ( $i = 1, \dots, n$ ), denoted as  $\pi_{i1}$ ,  $\pi_{i2}$  and  $\pi_{i3}$  respectively  
 (12, Chapter 8). We were interested in the association between these three  
 probabilities and the exposures, hence we used a nominal logistic regression

115 (or multinomial) model defined as

$$\begin{aligned}
 \hat{\pi}_{i1} &= \frac{1}{1 + \exp(r_{i2}) + \exp(r_{i3})}, & i = 1, \dots, n, \\
 \hat{\pi}_{ij} &= \frac{\exp(r_{ij})}{1 + \exp(r_{i2}) + \exp(r_{i3})}, & i = 1, \dots, n, j = 2, 3, \\
 r_{ij} &= \mathbf{x}_i^T \mathbf{b}_j, & i = 1, \dots, n, j = 2, 3,
 \end{aligned} \tag{1}$$

116 where  $\mathbf{x}_i$  is a set of exposures for row  $i$  of the data and  $\mathbf{b}_j$  is the vector of  
 117 parameters for outcome  $j$  ( $b_{j1}, \dots, b_{jp}$ ), where  $j = 2$  represents ICU discharge  
 118 and  $j = 3$  represents death. The above formulation satisfies the multinomial  
 119 assumption that  $\pi_{i1} + \pi_{i2} + \pi_{i3} = 1$ .

120 The exponential of  $b_{jk}$  gives the relative risk ratio, for a one unit increase  
 121 in the values of covariate  $k$ , of being in category  $j = 2, 3$  relative to category  
 122  $j = 1$  (staying), given that the other covariates are held constant. For  
 123 example, a value of  $\exp(b_{2,5}) = 2$  would mean that the relative risk of being  
 124 discharged would be twice as likely than staying when covariate 5 is increased  
 125 by one. A relative risk ratio is similar to an odds ratio, but is necessarily  
 126 more complicated because of the multiple response categories.

127 This nominal logistic regression model can be thought of as a discrete  
 128 time longitudinal survival model (13, Section 10.2.3) and is closely related to  
 129 a competing risks model (14). To realise this, consider that the multinomial  
 130 model estimates the probability of death or discharge on each day. Similarly,  
 131 if we used a competing risks model we would estimate the probability of  
 132 death or discharge in a short period of time. Previous work has shown the

133 similarity between a logistic longitudinal survival model (i.e.,  $j = 1, 2$ ) and  
 134 Cox regression (15). We have extended this similarity by changing the logistic  
 135 model to a nominal logistic model, and the Cox regression to a competing  
 136 risks model.

137 One advantage of using a nominal logistic model with a longitudinal struc-  
 138 ture is the ability to incorporate random effects. These are useful for mod-  
 139 elling heterogeneity and allow the model to account for some of the large un-  
 140 explained variation in length of stay. We considered models with a random  
 141 intercept for each patient admission, allowing the probability of discharge  
 142 and death to vary between admissions. The regression equation (1) becomes

$$r_{ij} = \mathbf{x}_i^T \mathbf{b}_j + z_{sj} I(s_i = s), \quad i = 1, \dots, n, j = 2, 3,$$

143 where  $z_{sj}$  is the random intercept for admission  $s$  for discharge ( $j = 2$ ) and  
 144 death ( $j = 3$ ). As before, we do not need to specify an intercept for the  
 145 reference category ( $j = 1$ ). The  $I()$  is an indicator function which matches  
 146 the admission number on row  $i$  of the data to admission  $s$ . We used a mul-  
 147 tivariate Normal distribution to create each admission's death and discharge  
 148 intercept

$$\mathbf{z}_s \sim \mathbf{N}(\mathbf{0}, \Omega), \quad s = 1, \dots, m,$$

149 where  $\Omega$  is a  $2 \times 2$  variance-covariance matrix and  $m$  is the total number of  
 150 subjects.

151 We also considered models with time-dependent covariates, allowing the  
 152 effect of MRSA infection on subsequent ICU stay to vary with the number  
 153 of days in the ICU when infected. To do this we changed the regression  
 154 equation (1) to

$$r_{ij} = \mathbf{x}_i^T \mathbf{b}_j + x'_i c_{jd} I(d_i = d), \quad i = 1, \dots, n, j = 2, 3, \quad (2)$$

155 where  $x'_i$  is a time-dependent exposure and  $d_i$  is the days since ICU entry for  
 156 row  $i$  of the data. The parameter  $c_{jd}$  is then the effect of  $x'_i$  on day  $d$ , and is  
 157 estimated separately for discharge ( $j = 2$ ) and death ( $j = 3$ ). We estimated  
 158 the  $c_{jd}$  parameters as Normally distributed random effects given by

$$c_{jd} \sim N(\mu_c, \sigma_c^2).$$

159 Because the number of patients not discharged or dead becomes small as  $d$   
 160 becomes large, we truncated the time-varying intercept after 21 days. So for  
 161  $d \geq 22$ ,  $c_{jd} = c_{j22}$ .

162 Equation (2) can also be used to model a lagged effect for a time-dependent  
 163 covariate if  $d$  is defined as the number of days since  $x'_i$  equalled  $X$ . This  
 164 lagged effect allows the effect of the covariate to change after a specific event  
 165 ( $x'_i = X$ ). In this analysis, we allowed the effect of MRSA infection to vary  
 166 with the time since first infected, because we were interested in whether the  
 167 effect of the MRSA infection on discharge waned with increasing time since  
 168 infection.

## 169 **Estimating the extra length of stay**

170 To calculate the excess length of stay due to infection on day  $d$  we subtracted  
171 the survivor functions from the day of infection onwards using

$$E(\text{excess LOS}|\text{MRSA on day } d) = \sum_{t=d}^m S(t|\text{MRSA on day } d) - S(t|\text{no MRSA}).$$

172 We only evaluate the sum up to some limit  $m$ , as for large values of  $t$  the  
173 survivor functions become very small. In this analysis we use a limit of  
174  $m = 21$  days. We estimated the survivor function at day  $t$  by multiplying  
175 the probabilities of staying from day 1 up to day  $t$ ,

$$S(t) = \pi_{j1}(t' = 1, \mathbf{x}_j) \times \pi_{j1}(t' = 2, \mathbf{x}_j) \times \dots \times \pi_{j1}(t' = t, \mathbf{x}_j)$$

176 where  $\mathbf{x}_j$  is a set of covariates (we have used a different notation to that above  
177 to emphasise the dependence of the probability on time and the covariates).  
178 We estimated the excess length of stay for an infection occurring during each  
179 of the first 21 days in ICU, and for three different Day 1 APACHE II scores:  
180 10, 20 and 30, reflecting a range of morbidity.

## 181 **Model fitting and building**

182 We fitted a number of different models using the model extensions detailed  
183 above using the same set of exposures for each model (Table 1). We selected  
184 the best fitting model using the deviance information criterion (DIC). A dif-

ference in DIC of 10 is considered substantial (<http://www.mrc-bsu.cam.ac.uk/bugs/winbugs/dicpage.shtml>).

The models were fitted in a Bayesian framework using the WinBUGS package (16), using vague priors for all unknown parameters. We used a vague Normal prior with zero mean and variance of 1000 for all regression parameters, and a gamma prior with a shape and inverse scale parameter of 0.001 for all inverse-variance parameters.

## Missing data

As shown in Table 1, there was some missing data for the TISS score, and just three missing scores for the day 1 APACHE II. The TISS scores were most often missing on the day of a patient’s discharge or death. To prevent these important days from being lost from the analysis we imputed the TISS scores using a random effect for each admission given by

$$\begin{aligned} x_{ik} &\sim N(\mu_i, \sigma_w^2), & i = 1, \dots, n, k = 1, \dots, m_i, \\ \mu_i &\sim N(\mu, \sigma_b^2), & i = 1, \dots, n, \end{aligned}$$

where  $m_i$  is the number of days observed for subject  $i$ ,  $\mu_i$  is the mean score for each subject, and  $\sigma_b^2$  and  $\sigma_w^2$  estimate the between- and within-subject variance, respectively. This imputation was made in WinBUGS in tandem with the estimation of the parameters governing discharge and death. In order to keep the regression model and imputation separate we used the

203 “cut” function (17).

## 204 RESULTS

205 There were 4569 separate admissions leading to 44,505 days spent on the  
206 ICU. Lengths of patient stays ranged from 0 to 363 days, and were highly  
207 skewed with a mean (SD) of 8.8 (14.1) days and a median (IQR) of 4 (2, 11).  
208 MRSA was cultured from 864 patients of which 335 developed an MRSA  
209 infection which led to 6696 infected days: 15.0% of the total patient-days on  
210 the ICU. One-hundred and six (31.6%) of the 335 admissions who developed  
211 an MRSA infection died, compared with 916 out of 4234 (21.6%) of the  
212 admissions without an MRSA infection.

213 We fitted seven different models to the data and they are compared using  
214 the DIC in Table 2. Model I had no random intercepts or time-dependent  
215 covariates (see table 1 for list of exposures). Model II built on Model I by  
216 including a time-dependent intercept to account for the fact that risk of death  
217 or discharge might vary during a patient’s stay on ICU. This decreased the  
218 DIC by 710 indicating a substantially improved model fit. The probabilities  
219 that a patient stayed, died or was discharged during the first 21 days in ICU  
220 are shown in Figure 1. The most notable feature is the change from a low  
221 probability of discharge of 0.08 on the day of admission (day 0) to a peak in  
222 discharge probability on day 1 of 0.29. After day 1 the daily probability of  
223 discharge gradually decreases with increasing stay. The probability of death

224 is small on any day, ranging between 0.01 and 0.02.

225 Model III extended Model II by adding random admission-specific in-  
226 tercepts to account for between-admission variation not explained by other  
227 covariates. This addition improved the model fit greatly as the DIC decreased  
228 by 520 (Table 2).

229 Model IV built on Model III by allowing the effect of MRSA infection  
230 on death and discharge to vary depending upon when it occurred over the  
231 first 21 days after ICU admission. This addition worsened the model fit as  
232 the DIC increased by 10 (Table 2). The time-dependent MRSA estimates  
233 for the daily relative risk ratios of discharge and death are shown in Figure  
234 2. MRSA infection was associated with a decreased risk of discharge, and  
235 this decrease was similar regardless of whether the MRSA infection occurred  
236 early or late in a patient’s stay. The mean relative risk ratio of discharge  
237 after becoming infected with MRSA was 0.78 (95% CI: 0.62, 0.97) relative  
238 to an MRSA free patient. Developing an MRSA infection had little direct  
239 effect on the risk of death ( $RRR = 1.12$ , 95% CI: 0.88, 1.38).

240 Model V extended Model III by allowing the effect of MRSA infection on  
241 death and discharge, to vary from the day the infection started to examine  
242 whether the effect waned over time. This addition improved the model fit as  
243 the DIC decreased by 30 (Table 2). The time-dependent MRSA estimates  
244 for discharge and death are shown in Figure 3. The mean relative risk ratio  
245 of discharge after an MRSA infection was 0.76 (95% CI: 0.60, 0.97) relative  
246 to an MRSA free patient. There was a slight decrease in the effect of an



247 MRSA infection with increasing time since infection: during the first five  
248 days after infection the mean relative risk ratio of discharge was 0.73, while  
249 10 days after infection it was 0.77. Again, there was little evidence that  
250 MRSA infection had a direct effect on the risk of death ( $RRR = 1.16$ , 95%  
251 CI: 0.95, 1.37). This result is considered further in the discussion.

252 Models I–V all adjusted for the daily TISS score. We were concerned that  
253 TISS score could be affected not only by the underlying severity of patient  
254 illness but also by MRSA infection. If this were the case, adjusting for the  
255 daily TISS score would bias the estimate of the effect of MRSA on death and  
256 discharge (18), possibly causing the model to miss a true association between  
257 MRSA and death. We therefore fitted two more models (Model VI and VII).  
258 Model VI was as Model V, but adjusted for day 1 TISS only, instead of daily  
259 TISS. The effect of MRSA infection on death changed little, but the relative  
260 risk ratio of discharge strengthened to 0.69 (95% CI: 0.55, 0.84). Model VII  
261 was as model III, but without any adjustment for TISS score, the effect on  
262 discharge was similar,  $RRR = 0.68$  (95% CI: 0.54, 0.82).

263 The risk ratios of death and discharge relative to staying from Model VII  
264 are shown in Table 3. The strongest reduction in the risk of discharge was  
265 associated with ventilation, while haemofiltration was associated with the  
266 strongest increase in the risk of death. There was little evidence of difference  
267 in the risks of discharge or death between the five specialty categories. The  
268 risk of discharge varied by day of the week, being significantly lower on the  
269 weekend compared to Wednesday.

270 Figure 4 shows the relative risk ratio of discharge and death after an  
271 MRSA infection for the seven different models. For models IV to VI the  
272 effect plotted is the mean over all times. Including a time-dependent intercept  
273 greatly changed the effect of MRSA infection as shown by the differences in  
274 relative risk ratios between models I and II. Adding a random intercept meant  
275 that the effect of MRSA significantly decreased the risk of discharge (Model  
276 III compared with Model II). Models IV and V had similar mean relative  
277 risk ratios to Model III, but with slightly wider credible intervals. Models  
278 VI and VII showed the strongest reduction in the risk of discharge risk after  
279 MRSA infection.

280 Figure 5 shows the mean excess length of stay due to an MRSA infection  
281 according to day 1 APACHE scores. For an infection on day 1, a patient  
282 with an APACHE II score of 10 would have a mean extra length of stay of  
283 0.3 days (95% CI: 0.1, 0.5). A sicker patient with an APACHE II score of 30  
284 would a longer stay of 1.2 days (95% CI: 0.5, 2.0).

## 285 DISCUSSION

286 MRSA infection had little direct effect on risk of death (Figure 4; model  
287 VII RRR = 1.14, 95% CI: 0.93, 1.39). However, all the models considered  
288 indicated that infection indirectly contributed to increased mortality. This  
289 occurs because patients with MRSA infections tend to stay longer in the ICU,  
290 and each day in the ICU has an associated mortality risk. Such an indirect

link has also been found between nosocomial pneumonia infection and death  
(19).

All seven multinomial models considered found that MRSA infection decreased the risk of discharge. While the magnitude of this effect varied considerably between models, the three models which gave (by some margin) the best fits to the data (III, IV and V) all yielded remarkably similar estimates: patients with MRSA infections had a relative risk of discharge (compared to staying) that was about 20% lower than that for patients without MRSA infections.

Additional stay attributed to the MRSA infection was found to be higher for sicker patients (as measured by the APACHE II score) and for infections occurring earlier in the ICU stay (Figure 5). The mean excesses are for all admissions, so infections occurring at later times have a much smaller attributable cohort and so cause less overall excess stays. Sicker patients have less physical reserve and may be less able to cope with an infection, hence their increased length of stay after infection compared with healthier patients.

One potential drawback of our approach is the retrospective nature of the infection diagnosis based on SIRS criteria, antibiotic start and culture of MRSA from a clinical site. This led to a diagnosis of MRSA infection in 335 (39%) of 864 patients colonized with MRSA, which although high is likely to be explained by the particular virulence of MRSA compared with other hospital bacteria and the hyperinvasive nature of the TW MRSA strain that

314 was circulating on the ICU at that time (9).

315 Our approach to estimating additional length of stay caused by hospital  
316 infections overcomes the pitfalls that affect much of the literature, and we  
317 believe it should therefore provide more reliable estimates. However, an  
318 alternative analytical approach would have been to use a multistate model  
319 (14, 19, 20).

320 Such multistate models can be used to model the flow of patients through  
321 a set of defined states. For example, patients may start in the “hospital en-  
322 try” state, some may subsequently move to an “infected” state, and then  
323 to a “discharged” state. However, an important advantage of the approach  
324 we used is the relative ease of incorporating lagged covariates and random  
325 effects. Nonetheless, the two approaches have similarities, and the multinomial model used in this paper can be thought of as a discrete time analogue  
326 of a multistate model (when comparable models could be fitted, they were  
327 in fact found to give very similar results). One potential drawback of the  
328 multinomial model is that the data must be equally spaced, and in our case  
329 all times were rounded to the nearest day. However, the model could be  
330 readily extended to smaller time-steps if required and data were available.

332 The aim of this work was to estimate the degree to which MRSA infection  
333 causes increased length of stay, rather than to simply document associations.  
334 This raises important issues about identifying confounders. Controlling for  
335 the time-dependent exposure of daily TISS score gave a better fit to the data  
336 (Table 2), but it is also likely that MRSA infection will have an effect on the

337 TISS score, particularly through prompting new antibiotic starts, catheter  
338 insertions and treatment with vasoactive agents. Therefore adjusting for  
339 the daily TISS score in the model would not only be unnecessary, it would  
340 be potentially actively harmful and introduce bias (18). This consideration  
341 motivated Models VI (which includes only the day 1 rather than the daily  
342 TISS score) and Model VII (without any TISS score), which are therefore  
343 not vulnerable to this problem. These models showed an increased effect of  
344 MRSA infection on discharge compared with the other models with time-  
345 dependent covariates (Figure 4) (18).

346 Being able to compare the fit of the models using the DIC is one of  
347 the advantages of using a Bayesian framework (Table 2). One surprising  
348 result was the reduction in the effective number of parameters from 2208 for  
349 Model V to 1604 for Model VI, when the only change was fitting TISS as  
350 a time-independent, instead of time-dependent, covariate (hence we might  
351 have expected a reduction of around 40 parameters). The large reduction in  
352 the effective number of parameters is due to the day 1 TISS score explaining  
353 a lot of the between-admission variation in the risk of discharge and death.  
354 This variation is no longer modelled by the random subject intercept, and so  
355 many less parameters are needed. Nonetheless, despite the poorer fit to data  
356 as measured by the DIC, knowledge of the likely causal pathways suggests  
357 that models VI and VII would give the most reliable estimate of the impact  
358 of MRSA infection on length of stay.

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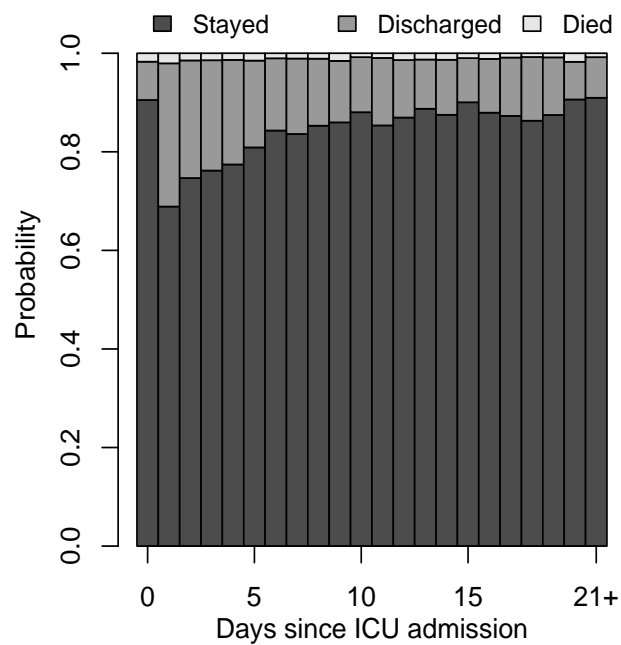
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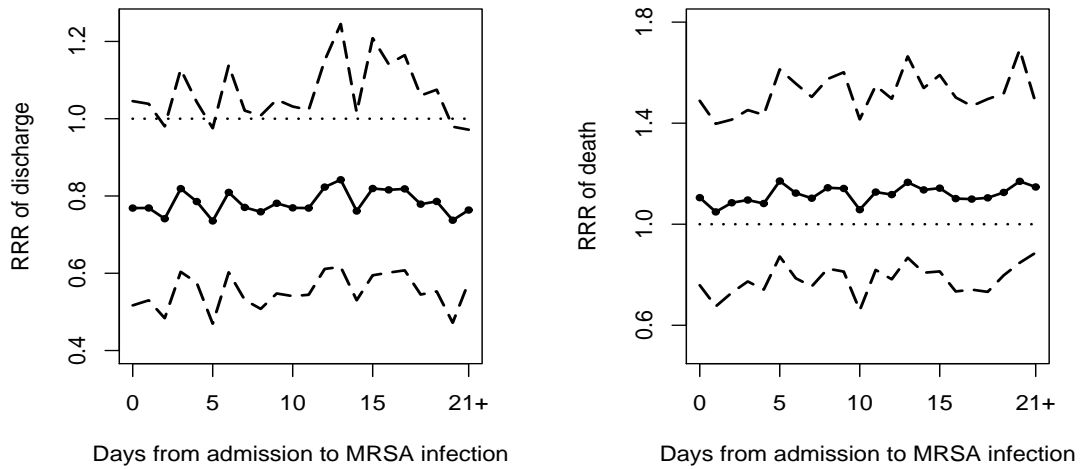
Figure 1: Probability that a patient stayed, was discharged or died by days since ICU admission (estimates from model II)



intensive care unit (ICU)

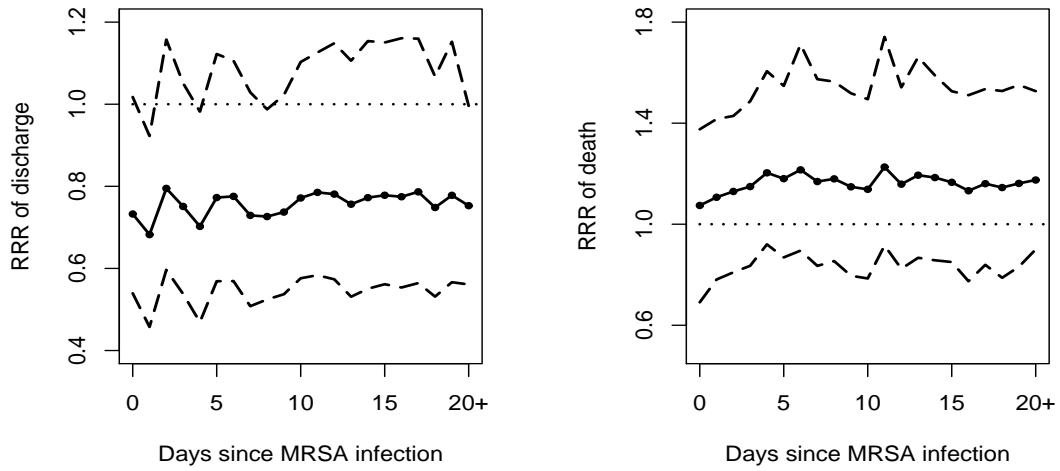
Mean probabilities from model II for a female patient aged 60, with a day 1 APACHE II of 20, daily TISS of 40, who is not ventilated or filtrated, in the specialty category of Medicine + Acute Renal Failure + Cardiology

Figure 2: Daily relative risk ratio of discharge and death from ICU relative to staying after an MRSA infection dependent on the time delay between admission and infection (estimates from model IV)



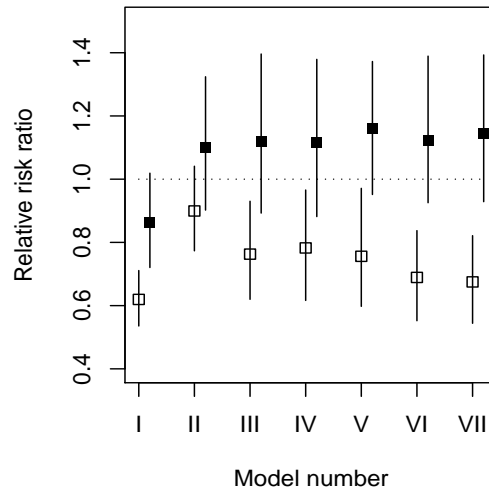
intensive care unit (ICU), Methicillin-resistant *Staphylococcus aureus* (MRSA), relative risk ratio (RRR)  
Mean relative risk ratio and 95% credible interval. Horizontal line at relative risk ratio of 1.

Figure 3: Daily relative risk ratio of discharge and death from ICU relative to staying after an MRSA infection by days since infection (estimates from model V)



intensive care unit (ICU), Methicillin-resistant *Staphylococcus aureus* (MRSA), relative risk ratio (RRR)  
Mean relative risk ratio and 95% credible interval. Horizontal line at relative risk ratio of 1.

Figure 4: Overall daily relative risk ratio of discharge and death from ICU relative to staying after developing an MRSA infection by model number



intensive care unit (ICU), Methicillin-resistant *Staphylococcus aureus* (MRSA)

Mean relative risk ratio and 95% credible interval. Open square for mean relative risk ratio of discharge, closed square for mean relative risk ratio of death. Horizontal line at relative risk ratio of 1.

Figure 5: Mean excess length of stay due to an MRSA infection by day of infection and Day 1 APACHE II score (estimates from model VII)

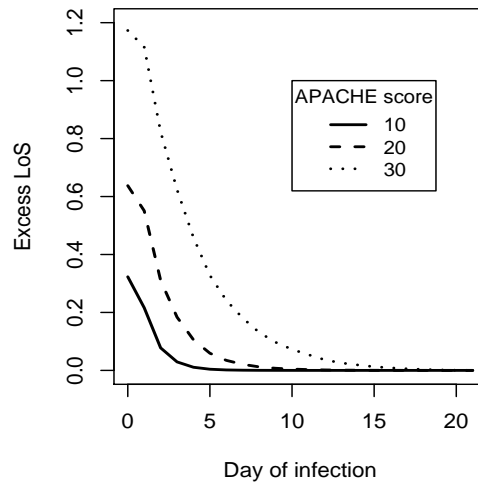


Table 1: Exposures Used and Descriptive Statistics

Covariate (category)	Time- dependent	Type	Missing	Statistics <sup>†</sup>
Age	No	Continuous	0	60 (17.5)
Sex (male)	No	Binary	0	2815 (61.6)
Speciality	No	Nominal	0	
Day of week	Yes	Nominal	0	
Day 1 APACHE II	No	Continuous	3 (0.1%)	17.2 (8.0)
TISS	Yes	Continuous	3844 (8.6%)	40.7 (13.4)
Ventilation (yes)	Yes	Binary	0	33,015 (74.2)
Haemofiltrated (yes)	Yes	Binary	0	7408 (16.6)
MRSA infection <sup>‡</sup> (yes)	Yes	Binary	0	6696 (15.0)

acute physiology and chronic health evaluation (APACHE), credible interval (CI), Methicillin-resistant

*Staphylococcus aureus* (MRSA), therapeutic intervention scoring system (TISS)

<sup>†</sup> Mean (standard deviation) for continuous covariates, number (% of patients) for sex and number (% of days) for binary time-dependent covariates

<sup>‡</sup> MRSA carried forward from day of infection to all subsequent days

Table 2: Comparing Different Models Using the Deviance Information Criterion

Model	Effective Number of parameters	Mean deviance	DIC	Difference in DIC <sup>†</sup>
I) No time-dependent covariates or random intercepts	333.0	27,070	27,400	
II) Model I + time-dependent intercept	382.6	26,310	26,690	710
III) Model II + random admission intercepts	2148	24,020	26,170	520
IV) Model III + time-dependent MRSA	2117	24,060	26,180	−10
V) Model III + lagged time-dependent MRSA	2208	23,930	26,140	30
VI) Model V − daily TISS + day 1 TISS	1640	25,370	27,370	−1230
VII) Model III − daily TISS	1649	25,750	27,400	−3340

deviance information criterion (DIC)

<sup>†</sup> Lower numbered model minus higher. A lower DIC indicates a better model fit; a difference in DIC of 10 is considered substantial.

Table 3: Relative Risk Ratios (and 95% credible intervals) of Daily Discharge and Death Relative to Staying. Estimates from Model VII.

Variable (units)	Discharge		Death	
	RRR	95% CI	RRR	95% CI
Age (10 year increase)	0.93	0.90, 0.96	1.13	1.08, 1.18
Sex (Male vs Female)	1.12	1.01, 1.25	0.81	0.71, 0.93
Day 1 APACHE II (5 point increase)	0.66	0.63, 0.69	1.32	1.25, 1.40
Ventilated (yes vs no)	0.05	0.04, 0.06	1.63	1.36, 1.99
Heamofiltration (yes vs no)	0.30	0.25, 0.36	1.80	1.56, 2.08
MRSA infection (yes vs no)	0.68	0.54, 0.82	1.14	0.93, 1.39
Speciality <sup>†</sup> (Surgery)	0.87	0.74, 1.01	1.07	0.89, 1.29
Speciality <sup>†</sup> (Cardiothoracic surgery)	0.94	0.80, 1.09	1.02	0.85, 1.23
Speciality <sup>†</sup> (Orthopaedics)	0.84	0.55, 1.24	1.21	0.67, 1.95
Speciality <sup>†</sup> (ITU referrals)	0.93	0.78, 1.11	1.14	0.93, 1.39
Day of the week <sup>‡</sup> (Monday)	0.89	0.77, 1.05	0.85	0.68, 1.07
Day of the week <sup>‡</sup> (Tuesday)	0.94	0.81, 1.11	0.95	0.76, 1.18
Day of the week <sup>‡</sup> (Thursday)	1.00	0.85, 1.17	0.91	0.72, 1.14
Day of the week <sup>‡</sup> (Friday)	1.06	0.92, 1.24	0.93	0.73, 1.17
Day of the week <sup>‡</sup> (Saturday)	0.72	0.62, 0.86	0.90	0.72, 1.13
Day of the week <sup>‡</sup> (Sunday)	0.63	0.53, 0.75	0.98	0.78, 1.24

acute physiology and chronic health evaluation (APACHE), credible interval (CI), Methicillin-resistant *Staphylococcus aureus* (MRSA), relative risk ratio (RRR), therapeutic intervention scoring system (TISS)

<sup>†</sup> Reference category = Medicine + Acute Renal Failure + Cardiology

<sup>‡</sup> Reference category = Wednesday